

## Lesson 2 – Improper to Mixed Numbers

**NC Objective:**

Recognise mixed numbers and improper fractions and convert from one form to the other and write mathematical statements  $> 1$  as a mixed number [for example  $2/5 + 4/5 = 6/5 = 1 \frac{1}{5}$ ]

**Resources needed:**

Differentiated Sheets  
Teaching Slides

**Vocabulary:**

Improper fractions, mixed numbers, convert, numerator, denominator, represent

Children convert improper fractions to mixed numbers for the first time. An improper fraction is a fraction where the numerator is greater than the denominator. A mixed number is a number consisting of an integer and a proper fraction. It is important for children to see this process represented visually to allow them to make the connections between the concept and what happens in the abstract.

**Key Questions:**

How many parts are there in a whole?

What do you notice happens to the mixed number when the denominator increases and the numerator remains the same?

What happens when the numerator is a multiple of the denominator?

★ Working Towards

This sheet shows six examples of improper fractions converted to mixed numbers using bar models. Each example includes a bar model, the original fraction, and the resulting mixed number.

- Tammy converts  $\frac{41}{4}$  into a mixed number using a bar model.  $\frac{41}{4}$  is the same as  $10 \frac{1}{4}$ .
- Isabella converts the improper fraction  $\frac{27}{8}$  into a mixed number using a bar model.  $\frac{27}{8}$  is the same as  $3 \frac{3}{8}$ .
- Mia converts the improper fraction  $\frac{57}{10}$  into a mixed number using a bar model.  $\frac{57}{10}$  is the same as  $5 \frac{7}{10}$ .
- Matthew converts the improper fraction  $\frac{42}{5}$  into a mixed number using a bar model.  $\frac{42}{5}$  is the same as  $8 \frac{2}{5}$ .
- Daniel converts the improper fraction  $\frac{25}{6}$  into a mixed number using a bar model.  $\frac{25}{6}$  is the same as  $4 \frac{1}{6}$ .
- Sienna converts the improper fraction  $\frac{39}{7}$  into a mixed number using a bar model.  $\frac{39}{7}$  is the same as  $5 \frac{4}{7}$ .

★★ Working Within

This sheet provides abstract fraction conversion problems. It includes two columns of problems, each with a fraction and a bar model for the student to complete.

- $\frac{37}{7}$  is the same as  $\square$
- $\frac{18}{3}$  is the same as  $\square$
- $\frac{31}{4}$  is the same as  $\square$
- $\frac{53}{8}$  is the same as  $\square$
- $\frac{46}{6}$  is the same as  $\square$
- $\frac{66}{5}$  is the same as  $\square$
- $\frac{21}{2}$  is the same as  $\square$
- $\frac{73}{6}$  is the same as  $\square$

Below these are two more columns of problems with bar models for coloring.

★★★ Greater Depth

This sheet includes coloring activities and word-based fraction problems. It features bar models for coloring and a list of words to be matched with fractions.

Choose the correct improper fraction and mixed number corresponding to each bar model. Remember that some fractions and numbers are extra.

- Eighty-four twelfth
- Six and six thirteenth
- Ninety-two seventh
- Eighty-four thirteenth
- Six and seven thirteenth
- Ninety-two thirteenth
- Seven and eight twelfth
- Ninety-two twelfth
- Seven and seven twelfth

On this sheet, they will use a completed bar model that represents improper fractions as a mixed number.

On this sheet, they will have an abstract fraction and are to draw a bar model themselves that represents the improper fractions as a mixed number.

On this sheet, children show their understanding by colouring a bar model and choosing the correct amount of bars to colour in.

They identify improper fractions written in words.

## Reasoning & Problem Solving

Represented here are some improper fractions which are then converted to mixed numbers. Spot and explain the mistakes.

Leanna says:  $\frac{15}{3}$  is less than  $\frac{15}{4}$  because 3 is less than 4.

Do you agree? Explain your answer using a bar model.

Represented here are some improper fractions which are then converted to mixed numbers. Spot and explain the mistakes.

Leanna says:  $\frac{15}{3}$  is less than  $\frac{23}{4}$  because 15 is less than 23.

Do you agree? Explain your answer using a bar model.

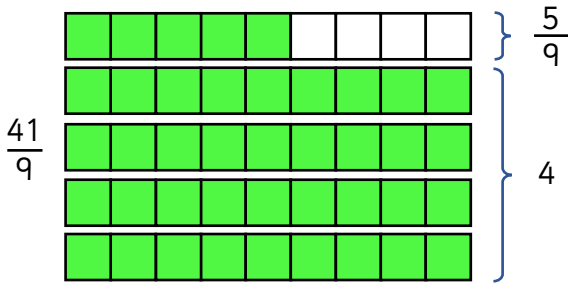
Represented here are some improper fractions which are then converted to mixed numbers. Spot and explain the mistakes.

Leanna says: Thirteen quarters is less than thirty-four thirtieths because thirteen is less than thirty-four.

Do you agree? Explain your answer using a bar model.

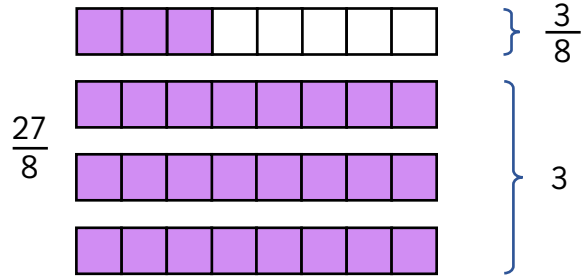


Tommy converts the improper fraction  $\frac{41}{9}$  into a mixed number using a bar model.



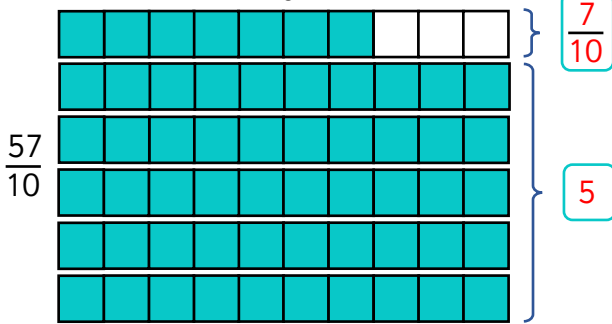
$\frac{41}{9}$  is the same as 4  $\frac{5}{9}$

Isabella converts the improper fraction  $\frac{27}{8}$  into a mixed number using a bar model.



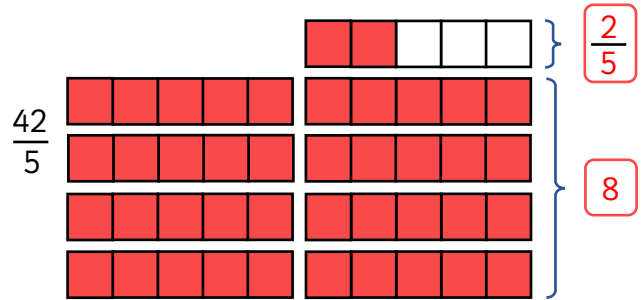
$\frac{27}{8}$  is the same as 3  $\frac{3}{8}$

Maisie converts the improper fraction  $\frac{57}{10}$  into a mixed number using a bar model.



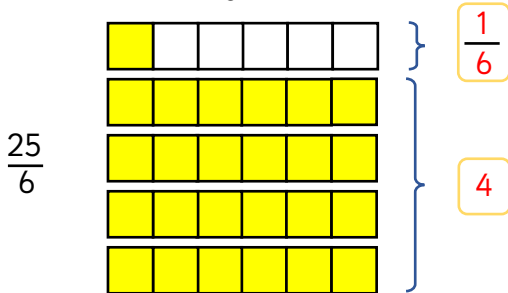
$\frac{57}{10}$  is the same as 5  $\frac{7}{10}$

Matthew converts the improper fraction  $\frac{42}{5}$  into a mixed number using a bar model.



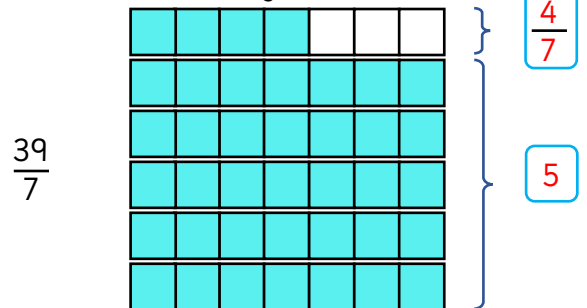
$\frac{42}{5}$  is the same as 8  $\frac{2}{5}$

Daniel converts the improper fraction  $\frac{25}{6}$  into a mixed number using a bar model.



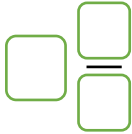
$\frac{25}{6}$  is the same as 4  $\frac{1}{6}$

Sienna converts the improper fraction  $\frac{39}{7}$  into a mixed number using a bar model.

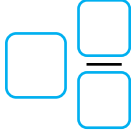


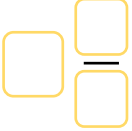
$\frac{39}{7}$  is the same as 5  $\frac{4}{7}$

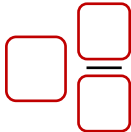
Convert the improper fractions into mixed numbers using bar models.

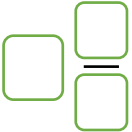
$\frac{37}{7}$  is the same as 

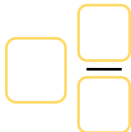
$\frac{19}{3}$  is the same as 

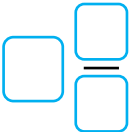
$\frac{31}{4}$  is the same as 

$\frac{53}{8}$  is the same as 

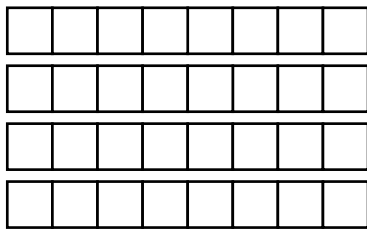
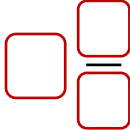
$\frac{44}{9}$  is the same as 

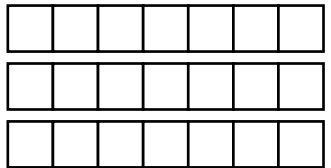
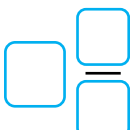
$\frac{66}{5}$  is the same as 

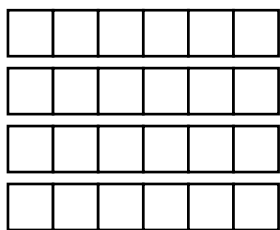

$\frac{21}{2}$  is the same as 

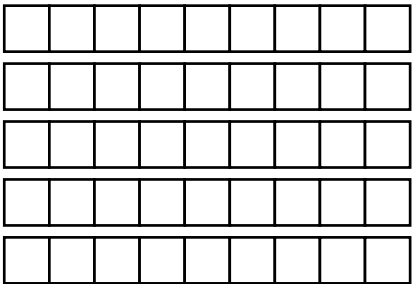
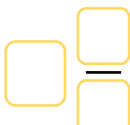
$\frac{73}{6}$  is the same as 

Colour each bar model according to the given improper fraction. Determine the corresponding mixed numbers.

  $\frac{25}{8}$  

$\frac{19}{7}$   

  $\frac{20}{6}$  

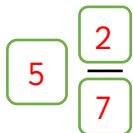
$\frac{39}{9}$   



Convert the improper fractions into mixed numbers using bar models.

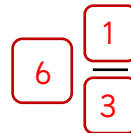
$$\frac{37}{7}$$

is the same as



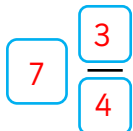
$$\frac{19}{3}$$

is the same as



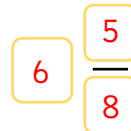
$$\frac{31}{4}$$

is the same as



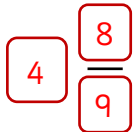
$$\frac{53}{8}$$

is the same as



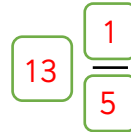
$$\frac{44}{9}$$

is the same as



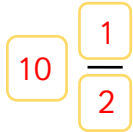
$$\frac{66}{5}$$

is the same as



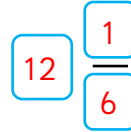
$$\frac{21}{2}$$

is the same as

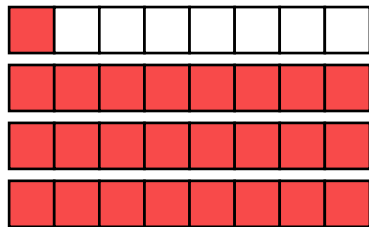


$$\frac{73}{6}$$

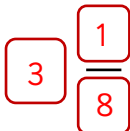
is the same as



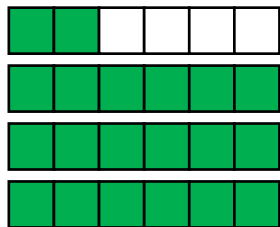
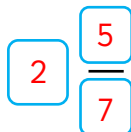
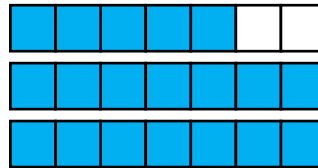
Colour each bar model according to the given improper fraction. Determine the corresponding mixed numbers.



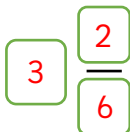
$$\frac{25}{8}$$



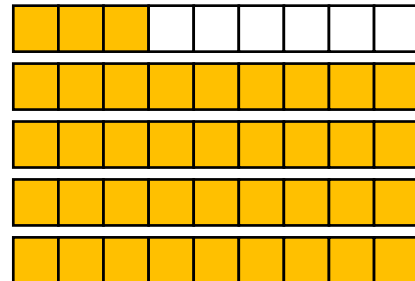
$$\frac{19}{7}$$



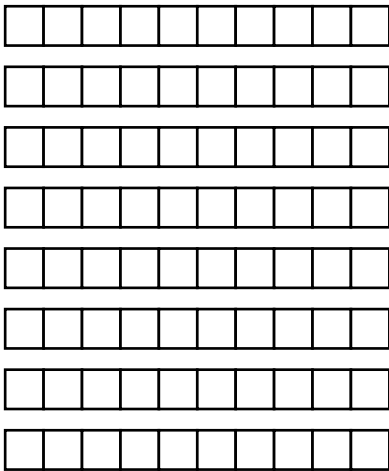
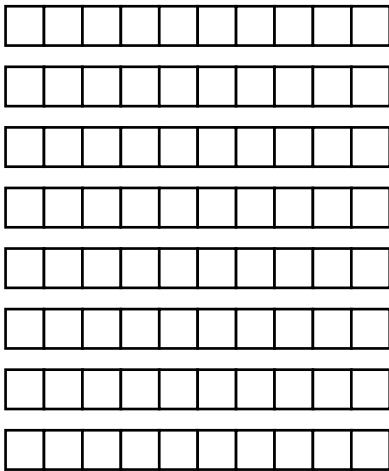
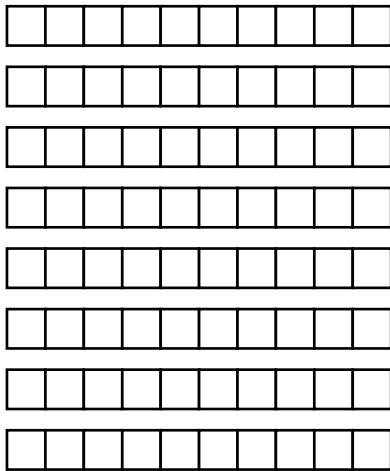
$$\frac{20}{6}$$












$$\frac{39}{9}$$



Colour each bar model according to the given improper fraction. Determine the corresponding mixed numbers.

|  |  |  |
|--|--|--|
|                      |                     |                    |
| $\frac{59}{8}$ is the same as <input type="text"/> $\frac{\text{ } = \text{ }}{\text{ } = \text{ }}$ | $\frac{52}{9}$ is the same as <input type="text"/> $\frac{\text{ } = \text{ }}{\text{ } = \text{ }}$ | $\frac{46}{7}$ is the same as <input type="text"/> $\frac{\text{ } = \text{ }}{\text{ } = \text{ }}$ |

Choose the correct improper fraction and mixed number corresponding to each bar model. Remember that some fractions and numbers are extra.

|                           |  |  |
|---------------------------|--|--|
| Eighty-four twelfths      |   | <input type="text"/><br><input type="text"/>                           |
| Six and six thirteenths   |  | <input type="text"/><br><input type="text"/>                           |
| Ninety-two sevenths       |  | <input type="text"/> $\frac{\text{ } = \text{ }}{\text{ } = \text{ }}$ |
| Eighty-four thirteenths   |  | <input type="text"/> $\frac{\text{ } = \text{ }}{\text{ } = \text{ }}$ |
| Six and seven thirteenths |  | <input type="text"/> $\frac{\text{ } = \text{ }}{\text{ } = \text{ }}$ |
| Ninety-two thirteenths    |  | <input type="text"/><br><input type="text"/>                           |
| Seven and eight twelfths  |  | <input type="text"/><br><input type="text"/>                           |
| Ninety-two twelfths       |  | <input type="text"/> $\frac{\text{ } = \text{ }}{\text{ } = \text{ }}$ |
| Seven and seven twelfths  |  | <input type="text"/> $\frac{\text{ } = \text{ }}{\text{ } = \text{ }}$ |



Colour each bar model according to the given improper fraction. Determine the corresponding mixed numbers.

|   |   |   |
|---|---|---|
|   |   |   |
| $\frac{59}{8}$ is the same as $7 \frac{3}{8}$ | $\frac{52}{9}$ is the same as $5 \frac{7}{9}$ | $\frac{46}{7}$ is the same as $6 \frac{4}{7}$ |

Choose the correct improper fraction and mixed number corresponding to each bar model. Remember that some numbers are extra.

|   |   |
|---|---|
|   |   |
| <div style="border: 1px solid red; border-radius: 10px; padding: 5px; display: inline-block;">Eighty-four thirteenths</div> | <div style="border: 1px solid red; border-radius: 10px; padding: 5px; display: inline-block;"><math>\frac{84}{13}</math></div>  |
| <div style="border: 1px solid red; border-radius: 10px; padding: 5px; display: inline-block;">Six and six thirteenths</div> | <div style="border: 1px solid red; border-radius: 10px; padding: 5px; display: inline-block;"><math>6 \frac{6}{13}</math></div> |
|   | <div style="border: 1px solid red; border-radius: 10px; padding: 5px; display: inline-block;"><math>\frac{92}{12}</math></div>  |
|   | <div style="border: 1px solid red; border-radius: 10px; padding: 5px; display: inline-block;"><math>7 \frac{8}{12}</math></div> |
|   | <div style="border: 1px solid red; border-radius: 10px; padding: 5px; display: inline-block;">Ninety-two twelfths</div>         |
|   | <div style="border: 1px solid red; border-radius: 10px; padding: 5px; display: inline-block;">Seven and eight twelfths</div>    |

Extra numbers

Seven and seven twelfths

Eighty-four twelfths

Six and seven thirteenths

Ninety-two sevenths

Ninety-two thirteenths



Represented here are some improper fractions which are then converted to mixed numbers.

Spot and explain the mistakes.

$$\frac{48}{9} = 5 \frac{6}{9}$$

$$\frac{36}{8} = 4 \frac{4}{8}$$

$$\frac{34}{10} = 2 \frac{4}{10}$$

Find the correct answers.

Leanna says:

$\frac{19}{3}$  is less than  $\frac{19}{4}$  because 3 is less than 4.



Do you agree?  
Explain your answer using a bar model.



Represented here are some improper fractions which are then converted to mixed numbers.

Spot and explain the mistakes.

$$\frac{48}{9} = 5 \frac{6}{9}$$

$$\frac{36}{8} = 4 \frac{4}{8}$$

$$\frac{34}{10} = 2 \frac{4}{10}$$

Find the correct answers.

Leanna says:

$\frac{19}{3}$  is less than  $\frac{19}{4}$  because 3 is less than 4.

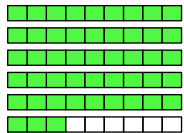



Do you agree?  
Explain your answer using a bar model.




Represented here are some improper fractions which are then converted to mixed numbers.

Spot and explain the mistakes.

$$\frac{48}{9} = 5 \frac{6}{9}$$


$$\frac{36}{8} = 4 \frac{4}{8}$$


$$\frac{34}{10} = 2 \frac{4}{10}$$


Find the correct answers.

Correct answers:

- $5 \frac{3}{9}$  (incorrect numerator)
- Incorrect bar model
- $3 \frac{4}{10}$  (incorrect whole and bar model)

Leanna says:

$\frac{19}{3}$  is less than  $\frac{19}{4}$  because 3 is less than 4.



Do you agree?

Explain your answer using a bar model.

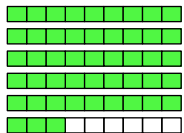
Leanna is incorrect.


$$\frac{19}{3} = 6 \frac{1}{3} \text{ is greater than } \frac{19}{4} = 4 \frac{3}{4}$$




Represented here are some improper fractions which are then converted to mixed numbers.

Spot and explain the mistakes.

$$\frac{48}{9} = 5 \frac{6}{9}$$


$$\frac{36}{8} = 4 \frac{4}{8}$$


$$\frac{34}{10} = 2 \frac{4}{10}$$


Find the correct answers.

Correct answers:

- $5 \frac{3}{9}$  (incorrect numerator)
- Incorrect bar model
- $3 \frac{4}{10}$  (incorrect whole and bar model)

Leanna says:

$\frac{19}{3}$  is less than  $\frac{19}{4}$  because 3 is less than 4.



Do you agree?

Explain your answer using a bar model.

Leanna is incorrect.

$$\frac{19}{3} = 6 \frac{1}{3} \text{ is greater than } \frac{19}{4} = 4 \frac{3}{4}$$



Represented here are some improper fractions which are then converted to mixed numbers.

Spot and explain the mistakes.

$$\frac{47}{9} = 5 \frac{7}{9}$$

$$\frac{39}{8} = 4 \frac{6}{8}$$

$$\frac{31}{7} = 4 \frac{3}{7}$$

Find the correct answers.

Leanna says:

$\frac{19}{3}$  is less than  $\frac{23}{4}$  because 19 is less than 23.



Do you agree?  
Explain your answer using a bar model.



Represented here are some improper fractions which are then converted to mixed numbers.

Spot and explain the mistakes.

$$\frac{47}{9} = 5 \frac{7}{9}$$

$$\frac{39}{8} = 4 \frac{6}{8}$$

$$\frac{31}{7} = 4 \frac{3}{7}$$

Find the correct answers.

Leanna says:

$\frac{19}{3}$  is less than  $\frac{23}{4}$  because 19 is less than 23.



Do you agree?  
Explain your answer using a bar model.



Represented here are some improper fractions which are then converted to mixed numbers.

Spot and explain the mistakes.

$$\frac{47}{9} = 5 \frac{7}{9}$$

$$\frac{39}{8} = 4 \frac{6}{8}$$

$$\frac{31}{7} = 4 \frac{3}{7}$$

Find the correct answers.

Correct answers:

- $5 \frac{2}{9}$  (incorrect numerator)
- $4 \frac{7}{8}$  (incorrect numerator)
- The bar model is incorrect

Leanna says:

$\frac{19}{3}$  is less than  $\frac{23}{4}$  because 19 is less than 23.



Do you agree?

Explain your answer using a bar model.

Leanna is incorrect.

$$\frac{19}{3} = 6 \frac{1}{3} \text{ is greater than } \frac{23}{4} = 5 \frac{3}{4}$$



Represented here are some improper fractions which are then converted to mixed numbers.

Spot and explain the mistakes.

$$\frac{47}{9} = 5 \frac{7}{9}$$

$$\frac{39}{8} = 4 \frac{6}{8}$$

$$\frac{31}{7} = 4 \frac{3}{7}$$

Find the correct answers.

Correct answers:

- $5 \frac{2}{9}$  (incorrect numerator)
- $4 \frac{7}{8}$  (incorrect numerator)
- The bar model is incorrect

Leanna says:

$\frac{19}{3}$  is less than  $\frac{23}{4}$  because 19 is less than 23.



Do you agree?

Explain your answer using a bar model.

Leanna is incorrect.

$$\frac{19}{3} = 6 \frac{1}{3} \text{ is greater than } \frac{23}{4} = 5 \frac{3}{4}$$



Represented here are some improper fractions which are then converted to mixed numbers.

Spot and explain the mistakes.

$$\frac{49}{9} = 6 \frac{4}{9}$$

$$\frac{35}{8} = 4 \frac{3}{8}$$

$$\frac{31}{6} = 5 \frac{1}{6}$$

Find the correct answers.

Leanna says:

Thirteen quarters is less than thirty-four thirteenths because thirteen is less than thirty-four.



Do you agree?  
Explain your answer using a bar model.



Represented here are some improper fractions which are then converted to mixed numbers.

Spot and explain the mistakes.

$$\frac{49}{9} = 6 \frac{4}{9}$$

$$\frac{35}{8} = 4 \frac{3}{8}$$

$$\frac{31}{6} = 5 \frac{1}{6}$$

Find the correct answers.

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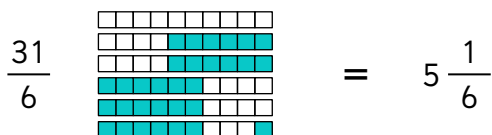
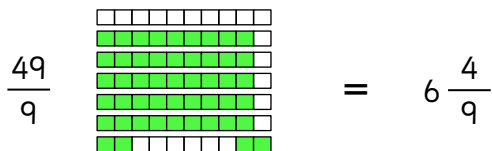


Do you agree?  
Explain your answer using a bar model.



Represented here are some improper fractions which are then converted to mixed numbers.

Spot and explain the mistakes.



Find the correct answers.

Correct answers:

- $5 \frac{4}{9}$  (incorrect whole)
- The bar model is incorrect
- The bar model is incorrect

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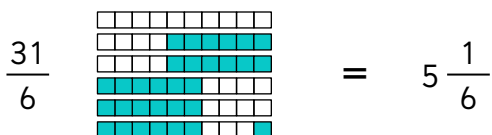
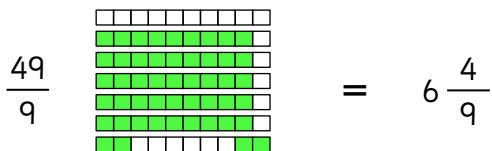
Leanna is incorrect.

$$\frac{13}{4} = 3 \frac{1}{4} \text{ is greater than } \frac{34}{13} = 2 \frac{8}{13}$$



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